

! For an efficient use of these tables, first read [HowTo.pdf](#).

T2.07A. Integrands of the form $\frac{1}{\sqrt{x(1-x)(a+bx)}}$ and $\frac{1}{\sqrt{(x-a)(x^2-2bx+c^2)}}$ on the intervals $(0, y)$, $(y, 1)$, (y, a) , and (a, y) .

$$1. \int_0^y \frac{dx}{\sqrt{x(1-x)(1-k^2x)}} = 2F(\arcsin \sqrt{y}, k), \quad 0 < y < 1.$$

$$2. \int_y^1 \frac{dx}{\sqrt{x(1-x)(k'^2+k^2x)}} = 2F(\arccos \sqrt{y}, k), \quad 0 < y < 1.$$

$$3. \int_y^1 \frac{dx}{\sqrt{x(1-x)(x-k'^2)}} = 2F\left(\arcsin \frac{\sqrt{1-y}}{k}, k\right), \quad 0 < y < 1.$$

$$4. \int_0^y \frac{dx}{\sqrt{x(1+x)(1+k'^2x)}} = 2F(\arctan \sqrt{y}, k), \quad 0 < y < 1.$$

$$5. \int_0^y \frac{dx}{\sqrt{x[1+x^2+2(k'^2-k^2)x]}} = F(2 \arctan \sqrt{y}, k), \quad 0 < y < 1.$$

$$6. \int_y^1 \frac{dx}{\sqrt{x[k'^2(1+x^2)+2(1+k^2)x]}} = F\left(\frac{\pi}{2} - 2 \arctan \sqrt{y}, k\right), \quad 0 < y < 1.$$

$$7. \int_a^y \frac{dx}{\sqrt{(x-a)(x^2-2bx+c^2)}} = \frac{1}{\sqrt{p}} F\left(2 \arctan \sqrt{\frac{y-a}{p}}, \sqrt{\frac{p+b-a}{2p}}\right), \quad a < y,$$

$$\text{where } p = \sqrt{a^2 - 2ab + c^2}.$$

$$8. \int_y^a \frac{dx}{\sqrt{(a-x)(x^2-2bx+c^2)}} = \frac{1}{\sqrt{p}} F \left(2 \arctan \sqrt{\frac{a-y}{p}}, \sqrt{\frac{p-b+a}{2p}} \right), \quad y < a,$$

where $p = \sqrt{a^2 - 2ab + c^2}$.
