

! For an efficient use of these tables, first read [HowTo.pdf](#).

**T2.14C.** Integrands of the form  $\sqrt{(a^2 \pm x^2)(x^2 \pm b^2)}$  and  $\sqrt{(a^2 \pm x^2)(x^2 \pm b^2)}$  on the interval  $(0, y)$ .

Notation used:  $\alpha = \arctan \frac{y}{b}$ ,  $\gamma = \arcsin \frac{y}{b} \sqrt{\frac{a^2 + b^2}{a^2 + y^2}}$ ,  $\eta = \arcsin \frac{y}{b}$ ,

$$q = \frac{\sqrt{a^2 - b^2}}{a}, \quad r = \frac{b}{\sqrt{a^2 + b^2}}, \quad t = \frac{b}{a}.$$

$$1. \int_0^y \sqrt{(x^2 + a^2)(x^2 + b^2)} dx = \frac{a}{3} \{2b^2 F(\alpha, q) - (a^2 + b^2)E(\alpha, q)\} \\ + \frac{y}{3} (y^2 + a^2 + 2b^2) \sqrt{\frac{a^2 + y^2}{b^2 + y^2}}, \quad a > b, y > 0.$$

$$2. \int_0^y \sqrt{(a^2 + x^2)(b^2 - x^2)} dx = \frac{1}{3} \sqrt{a^2 + b^2} \{a^2 F(\gamma, r) - (a^2 - b^2)E(\gamma, r)\} \\ + \frac{y}{3} (y^2 + 2a^2 - b^2) \sqrt{\frac{b^2 - y^2}{a^2 + y^2}}, \quad a \geq y > 0.$$

$$3. \int_0^y \sqrt{(a^2 - x^2)(b^2 - x^2)} dx = \frac{a}{3} \{(a^2 + b^2)E(\eta, t) - (a^2 - b^2)F(\eta, t)\} \\ + \frac{y}{3} \sqrt{(a^2 - y^2)(b^2 - y^2)}, \quad a > b \geq y > 0.$$


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