

! For an efficient use of these tables, first read [HowTo.pdf](#).

T3.13A. Integrands of the form $\frac{1}{x^4 \sqrt{(a^2 \pm x^2)(b^2 \pm x^2)}}$ on the interval (y, ∞) .

Notation used: $\beta = \arctan \frac{a}{y}$, $\xi = \arcsin \sqrt{\frac{a^2 + b^2}{a^2 + y^2}}$, $\nu = \arcsin \frac{a}{y}$,

$$q = \frac{\sqrt{a^2 - b^2}}{a}, \quad s = \frac{a}{\sqrt{a^2 + b^2}}, \quad t = \frac{b}{a}.$$

$$1. \int_y^\infty \frac{dx}{x^4 \sqrt{(x^2 + a^2)(x^2 + b^2)}} = \frac{1}{3a^3b^4} \{2(a^2 + b^2)E(\beta, q) - b^2F(\beta, q)\} \\ + \frac{a^2b^2 - y^2(2a^2 + b^2)}{3a^2b^4y^3}, \quad a > b, y > 0.$$

$$2. \int_y^\infty \frac{dx}{x^4 \sqrt{(x^2 + a^2)(x^2 - b^2)}} = \frac{1}{3a^4b^4\sqrt{a^2 + b^2}} \{2(a^4 - b^4)E(\xi, s) + b^2(2b^2 - a^2)F(\xi, s)\} \\ - \frac{a^2b^2 + y^2(2a^2 - b^2)}{3a^2b^4y^3} \sqrt{\frac{y^2 - b^2}{y^2 + a^2}}, \quad y \geq b > 0.$$

$$3. \int_y^\infty \frac{dx}{x^4 \sqrt{(x^2 - a^2)(x^2 - b^2)}} = \frac{1}{3a^3b^4} \left\{ (2a^2 + b^2)F(\nu, t) - 2(a^2 + b^2)E(\nu, t) \right. \\ \left. + \frac{ab^2}{y^3} \sqrt{(y^2 - a^2)(y^2 - b^2)} \right\}, \quad y \geq a > b > 0.$$
