

! For an efficient use of these tables, first read [HowTo.pdf](#).

T3.26C. Integrands involving exponentials and arbitrary powers of $(a + bx)$ on the interval $(1, \infty)$.

$$1. \int_1^\infty (x^2 - 1)^{\nu-1} e^{i\mu x} dx = \begin{cases} i \frac{\sqrt{\pi}}{2} \left(\frac{2}{\mu}\right)^{\nu-1/2} \Gamma(\nu) H_{1/2-\nu}^{(1)}(\mu), & \Im\{\mu\} > 0, \Re\{\nu\} > 0, \\ -i \frac{\sqrt{\pi}}{2} \left(-\frac{2}{\mu}\right)^{\nu-1/2} \Gamma(\nu) H_{1/2-\nu}^{(2)}(-\mu), & \Im\{\mu\} < 0, \Re\{\nu\} > 0. \end{cases}$$

$$2. \int_1^\infty (x^2 - 1)^{\nu-1} e^{-\mu x} dx = \frac{1}{\sqrt{\pi}} \left(\frac{2}{\mu}\right)^{\nu-1/2} \Gamma(\nu) K_{\nu-1/2}(\mu), \quad |\arg \mu| < \frac{\pi}{2}, \Re\{\nu\} > 0.$$

$$3. \int_1^\infty \frac{(\sqrt{x^2 - 1} + x)^\nu + (\sqrt{x^2 - 1} - x)^{-\nu}}{\sqrt{x^2 - 1}} e^{-\mu x} dx = 2K_\nu(\mu), \quad \Re\{\mu\} > 0.$$

$$4. \int_1^\infty \frac{(x + \sqrt{x^2 - 1})^{2\nu} + (x - \sqrt{x^2 - 1})^{2\nu}}{\sqrt{x(x^2 - 1)}} e^{-\mu x} dx = \sqrt{\frac{2\mu}{\pi}} K_{\nu+1/4}\left(\frac{\mu}{2}\right) K_{\nu-1/4}\left(\frac{\mu}{2}\right),$$

$\Re\{\mu\} > 0.$
